

Optimal Speed Control of Hybrid Stepper Motors through Integrating PID Tuning with LFD-NM Algorithm

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Abstract:

In order to regulate the speed of hybrid stepper motors (HSM), this work presents an optimally tuned proportional-integral-derivative (PID) controller. The combination of algorithms known as the combined Levy flight distribution and Nelder Mead (LFD-NM) method essentially considers it unique to tune the PID. The accurate local search properties of the Nelder Mead (NM) technique are combined with the exploratory capabilities of the Levy flight distribution (LFD) algorithm in this method. A combination LFD-NM approach improves PID controller parameter optimisation efficiency by striking a balance between exploration and exploitation. The efficacy of the suggested method is validated by comparative simulations against the original LFD algorithm and many metaheuristic algorithms including cuckoo search and genetic algorithms. The assessment of performance includes statistical testing, robustness analysis, management of load disturbances, evaluation of energy efficiency, assessment of transient and frequency responses, and consideration of control signal constraints. Additional experimental verification confirms that a recommended LFD-NM-based PID controller is successful. Analyses conducted in comparison with the latest PID controllers demonstrate its exceptional efficacy in attaining ideal control over the speed of hybrid stepper motors (HSM).

1. Introduction

Stepper motors, invented in the 19th century, found their modern form thanks to Thomas and Fleischauer in 1957 [1]. These motors are prevalent across various industries due to their exceptional precision in controlling positioning [1]. Their operation relies on a pulse system, dictating the step-by-step rotation of the shaft [2]. Stepper motors offer several advantages over their counterparts, including unmatched precision, straightforward control methods, high reliability, and efficient heat dissipation [3-5]. These benefits make them ideal for applications in automated

machinery, computer peripherals, and digital equipment [6,7]. Precise speed control is vital for many stepper motor applications. Compared to other motor types, stepper motors excel in this area [8]. Traditionally, PID controllers have been the go-to choice for stepper motor speed control due to their simplicity, affordability, and dependable performance [9-16]. However, optimizing PID controllers for peak performance can be a complex task [17-21].

Recent advancements have seen a rise in using metaheuristic algorithms for PID controller tuning. These algorithms efficiently search for the optimal PID controller settings without requiring deep system knowledge [22-26]. This document

proposes a new approach that integrates the Levy Flight Distribution (LFD) algorithm with Nelder Mead (NM) simplex search to improve PID controller optimization for stepper motors [27-40, 41]. This approach aims to strike a balance between exploration, where the algorithm searches for new possibilities, and exploitation, where it refines promising areas identified during the optimization process.

2. Research Approach

The development of specialised algorithms has great potential to solve difficult control systems and optimisation issues. In order to present a hybrid strategy in this field, this endeavour combines the Nelder Mead (NM) and Levy flight distribution (LFD) algorithms. The main goal is to provide a novel algorithmic framework that efficiently strikes a balance between exploration and exploitation in order to improve optimisation capabilities.

The recommended algorithm, known as LFD-NM, will also be used in this study to create and build a PID tuned controller specifically designed for a hybrid stepper motor (HSM) speed control system. By aiming to maximise the integral of time-weighted absolute error (ITAE) objectives function, the LFD-NM method is expected to perform better than other widely used algorithms in this field.

The graphical depiction of the performance evaluation technique is shown in Figure 1. To confirm the efficacy of the suggested strategy, a number of studies will be carried out, including testing with statistics, load disturbance assessments, robustness evaluations, and time domain analysis and frequency domain analysis. These evaluations seek to verify the superiority of the LFD-NM algorithm by contrasting it with its original form and with algorithms such as the genetic algorithm (GA) and cuckoo search algorithm (CS).

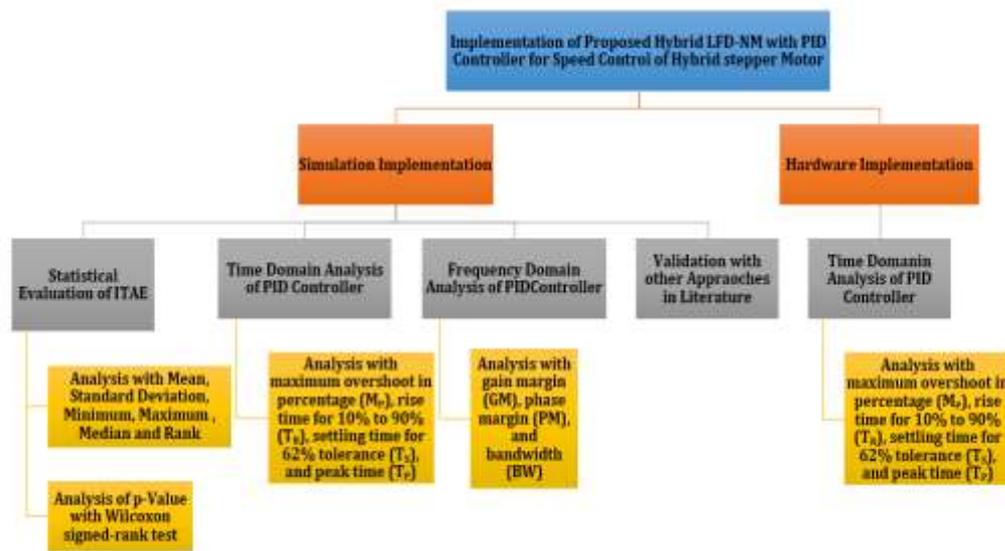


Figure 1. Proposed Performance Analysis Approach of Study

The ultimate evaluation will offer more proof of the dominance of the combined algorithm in accomplishing optimisation goals utilising a different, commonly-used time domain-based objective function. By achieving these specific goals, the research aims to promote innovation and development in related fields by making a contribution to optimisation algorithm and control system improvements.

3. Proposed LFD-NM based PID Controller for Speed Control of HSM

In order to overcome the inherent limitations of each algorithm, the Levy flight distribution (LFD) and Nelder Mead (NM) algorithms are integrated. This approach aims to balance exploration and

exploitation in optimisation tasks, specifically when it comes to adjusting the limits of PID controller for a hybrid stepper motor (HSM).

Despite being well-known for its robust exploratory capabilities, the LFD algorithm's very poor local search performance frequently prevents it from being fully utilised. On the other hand, the LFD algorithm has wider exploration capabilities, whilst the NM approach is superior in local search. This disparity provides the impetus for creating the LFD-NM algorithm, which combines the best features of both methodologies. When the LFD-NM algorithm is used for optimisation problems, it effectively combines the complementary features of the LFD and NM algorithms to give a balanced approach by seamlessly combining the stages of

exploration and exploitation. The choice of a suitable objective function is essential for maximising a system's stability and dynamic reaction, which in turn affects the likelihood of attaining better system performance. Since it can accurately represent both transient and steady-state performance indicators, the integral of time-weighted absolute error (ITAE) was selected as the goal function for this investigation. Furthermore, the gain parameters of the PID controller were limited to values within the range of [0.001, 20], in order to ensure a practical parameter search space.

$$ITAE = \int_0^T |(\omega(t)) - (\omega_{ref})| t. dt \quad (1)$$

The implementation technique of the suggested LFD-NM algorithm for changing the speed regulation of the PID-controlled hybrid Stepper motor system is as follows:

Step 1: Initialization of Parameters

This step involves establishing the parameters needed for the NM and LFD algorithms. Step sizes, population sizes, convergence criteria, and other algorithm-specific parameters are examples of these parameters.

Step 2: Creating a Random Population

A random population is generated using the gain parameters for proportional, integral, and derivative gain, which represent potential solutions. The first collection of potential solutions for the optimisation procedure is this random population.

Step 3: Iterative Algorithm Execution of LFD-NM

An iterative algorithm is used to run the LFD-NM method. In every iteration:

- ❖ **LFD Exploration:** The solution space is explored using the LFD algorithm. It entails using LFD operators, which are intended to make global exploration easier, to generate new candidate solutions.
- ❖ **Exploitation using NM:** Local exploitation is done using the NM algorithm following the exploration phase (Takenaga et al. 2023). This entails employing the NM simplex search method to iteratively update the solutions acquired from the LFD phase in order to improve them.
- ❖ **Fitness Function Evaluation:** The fitness function is assessed for each candidate solution found using the LFD-NM method. The ITAE, which measures the effectiveness of the PID-controlled motor speed system, serves as the fitness function in this instance.

Step 4: Termination Criteria

Until a predetermined termination criterion is satisfied, the iterative procedure is carried out.

Usually, this criterion is dependent on the number of iterations that can be reached.

Step 5: Best-performing Parameter Selection

The algorithm stops when the termination requirement is satisfied, and the candidate solution with the best-performing PID gain parameters is chosen using the lowest ITAE value. The PID controller's optimised settings are represented by these particular parameters.

Step 6: Hybrid Stepper Motor Speed System Implementation

In the context of HSM speed regulation, the integration of a Tuned PID controller within the system is pivotal, with its parameters fine-tuned using the optimal PID gain parameters determined through the LFD-NM algorithm. These parameters intricately govern the behaviour of the PID controller, directly influencing the system's efficacy in maintaining desired speeds. The proposed methodology adeptly exploits the complementary strengths of the NM and LFD algorithms, efficiently navigating the solution space. Through this integration, the algorithm meticulously seeks out the optimal PID parameters for HSM speed regulation, guided by the ITAE objective function. This iterative optimization process continuously refines the PID parameters, ensuring a gradual convergence towards an optimal solution that markedly enhances the system's speed regulation performance. By dynamically adjusting and updating the PID parameters based on the ITAE objective function, the algorithm facilitates precise and reliable speed regulation in high-speed machining applications, thereby underscoring its significance in optimizing system performance and efficiency.

4. Performance of LFD-NM Implementation on Speed Control of HSM

In the analysis, the original LFD algorithm, the Cuckoo search algorithm (CS) [42-58], and the Genetic Algorithm (GA) [59], two other well-known optimisation algorithms, were put to rigorous testing alongside the proposed LFD-NM algorithm. The goal was to demonstrate the proposed algorithm's greater performance in maximising a hybrid stepper motor's speed control. The proposed approach was built up with certain parameter settings that were carefully selected to guarantee an impartial and thorough study, as shown in Table 1 and 2. These constraints placed on the proportional (K_P), integral (K_I), and derivative (K_D) terms of the PID controller fell between [0.001, 20]. This allowed for adequate

solution space exploration while still preserving practical viability in the context of HSM speed control. Each algorithm optimisation process was carried out across 25 separate runs, enabling a reliable statistical analysis.

Table 1. Parameters of Proposed Algorithms

Algorithm	LFD-NM
Size of Population	20
Threshold	2
Step Size Control Parameter (Csv)	0.5
Power Law Exponent (b)	1.5
Learning Rate (al)	10
Factor of Reflection (a)	1
Factor of Expansion (g)	2
Factor of Contraction for Outside Contraction (d1)	0.9
Factor of Contraction for Inside Contraction (d2)	0.1
Factor of Shrinkage (d)	0.5

Moreover, a termination condition was developed in order to standardise the comparison: the optimisation process ended when the maximum number of iterations reached 100. By ensuring a uniform evaluation framework for all algorithms, this termination criteria made it possible to compare their performances in a meaningful way. An additional factor taken into account throughout the assessment was the optimisation process's effectiveness. For every algorithm, the average amount of time that passed between optimisation iterations was noted. The average elapsed time per iteration for the proposed LFD-NM method was 5.4 seconds, which was somewhat faster than the average of 4.9 seconds for the original LFD algorithm, according to the results. In the meanwhile, the average elapsed durations per iteration for the CS and GA algorithms were 3.9 and 3.6 seconds, respectively.

The performance characteristics of each algorithm in the Hybrid Stepper motor speed control system optimisation were thoroughly understood due to these meticulously planned experiments and studies. The documented information not only made a comparative analysis easier, but it also clarified the effectiveness and processing requirements of every algorithm, offering insightful information about the choice and use of optimisation algorithms.

4.1 Statistical evaluation of performance

The study's statistical analysis sought to offer a thorough grasp of the effectiveness of the various algorithms used for HSM speed control. With the use of objective function of the integral of time-weighted absolute error (ITAE), a number of

statistical parameters, including mean of ITAE, standard deviation of ITAE, minimum, maximum, and median values of ITAE, were derived for the analysis. These metrics are important measures of how well the algorithms work and how well they can control the speed of the HSM motor.

The proposed LFD-NM method consistently beats the other algorithms across all analysed parameters, as can be seen by looking at the statistical results shown in Table 3. The LFD-NM method outperforms the LFD, CS, and GA as shown by the mean of ITAE, standard deviation of ITAE, minimum, maximum, and median values of ITAE that were achieved. The LFD-NM method, in particular, has the lowest worst value, indicating that it may perform better even in the face of difficult circumstances or anomalies. The algorithm also shows the best values for the average and standard deviation, which suggests that it performs with more consistency and dependability.

Table 2. ITAE Statistical Analysis Parameters

Algorithm	Mean	Standard Deviation	Minimum	Maximum	Median	Rank
LFD-NM	0.002	0.58* 10 ⁻⁴	0.0015	0.0017	0.0015	1
LFD	0.004	1.24* 10 ⁻⁴	0.0039	0.0042	0.0038	2
CS	0.005	1.73* 10 ⁻⁴	0.0049	0.0054	0.0051	3
GA	0.01	4.09* 10 ⁻⁴	0.009	0.011	0.0099	4

The supremacy of the LFD-NM algorithm is further reinforced by the algorithm ranking according to statistical performance. Among the compared algorithms, the LFD-NM algorithm achieves the highest rank, indicating that it is the optimal choice for motor speed control based on the ITAE objective function. The algorithm is an attractive option for real-world applications because of its ability to continuously give optimal performance across various parameters, as demonstrated by this rating.

4.2 Evaluation of time domain and frequency domain performance

The work provides insight into the performance of PID-controlled HSM speed systems in the time and frequency domains utilising a variety of optimisation methods, such as LFD, CS, GA-tuned PID controllers, and the LFD-NM algorithm. Transfer functions were produced using matching PID-controlled HSM speed systems for LFD, CS, GA algorithm tuned PID controllers, and proposed

LFD-NM PID controllers, respectively, by replacing the gain values found in Table 4, 5.

Table 3. Gain Parameters

PID Parameters	LFD-NM	LFD [40]	CS [58]	GA [59]
K_P	19.56	17.21	13.93	8.86
K_I	5.16	4.41	8.08	6.06
K_D	3.41	3.08	2.18	1.46

The time domain performance analysis's findings are shown in Table 6, which also includes peak time (T_P), rising time for 10% to 90% (T_R), settling time for 62% tolerance (T_S), and maximum overshoot in percentage (M_P). Figure 2 shows the relative speed step responses of the motor speed systems under the direction of various algorithms.

Table 4. Time Domain Performance Parameters

Time Domain Parameters	LFD-NM	LFD	CS	GA
M_P (%)	0	0.08	1.91	2.61
T_R (sec)	0.055	0.064	0.083	0.125
T_S (sec)	0.092	0.114	0.131	0.889
T_P (sec)	0.157	0.294	0.270	0.451

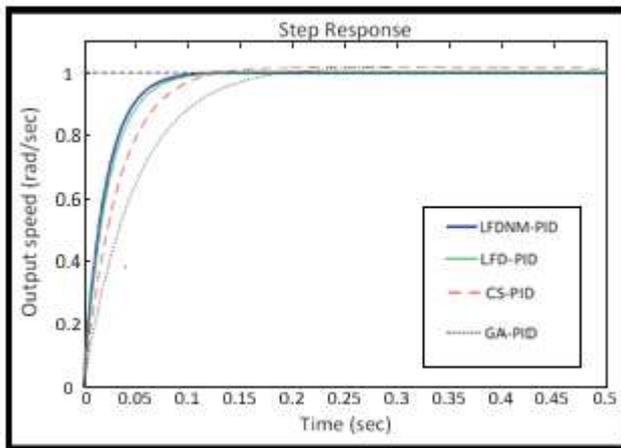


Figure 2. Time Domain Step Response Analysis

The LFD-NM-based PID controller that has been proposed has better temporal response characteristics than the LFD, CS and GA tuned PID controllers. These features include null overshoot, shorter rise time, settling time, and peak time, as can be seen in the table and figure 3. This suggests that the HSM speed control system can benefit from improved stability, quicker damping, and no overshoot provided by the proposed controller structure.

A comparison of the frequency domain characteristics for PID based on the LFD-NM algorithm and other approaches also includes gain margin (GM), phase margin (PM), and bandwidth (BW). The LFD-NM algorithm-tuned motor system has the maximum stability in terms of frequency

response, as shown in the related figure 4 and table 4.

Table 5. Frequency Domain Performance Parameters

Frequency Domain Parameters	LFD-NM	LFD	CS	GA
GM (dB)	∞	∞	∞	∞
P_M (deg.)	180	180	171.01	169.05
BW (Hz)	47.34	42.62	30.93	20.69

For HSM speed regulation, the comprehensive analysis of performance measures in the time and frequency domains validates the improved effectiveness of the LFD-NM algorithm-based tuning of PID controller. It is a viable choice for real-world applications requiring high-performance speed control systems because, in comparison to other algorithms, it can provide precise, fast, and dependable control.

5. Real Time Implementation of LFD-NM on Speed Control of HSM

The LFD-NM-based PID controller's performance and practicality were confirmed by an essential experimental validation procedure. An experimental setup was used during the study's validation phase to confirm the results of the simulations. This method combines the Levy Flight Distribution (LFD) algorithm with Nelder Mead (NM) simplex search (LFD-NM). To validate this approach, they constructed a physical testbed consisting of the stepper motor, driver, power supply and a data acquisition system (DAQ). This setup interfaced with a LabVIEW control program for real-time control and data collection.

The LabVIEW program implemented the LFD-NM optimized PID algorithm and sent speed commands to the motor driver. A magnetic encoder provided feedback on the motor's actual speed, closing the control loop. The performance of the LFD-NM PID controller is compared to conventionally optimized controllers. The motor's response to speed commands, including the desired speed, rising time, settling time and overshoot beyond the target speed is also measured. Finally, they compared experimental results with simulations to verify the accuracy of their LFD-NM approach. Experimental results were achieved at a commanded speed. The improved performance of the suggested LFD-NM-based PID tuning is confirmed by an exact correlation between the simulation and experiment results. These consistent results from modelling and experimentation provide more evidence for the effectiveness of the proposed controller architecture in controlling HSM speed.

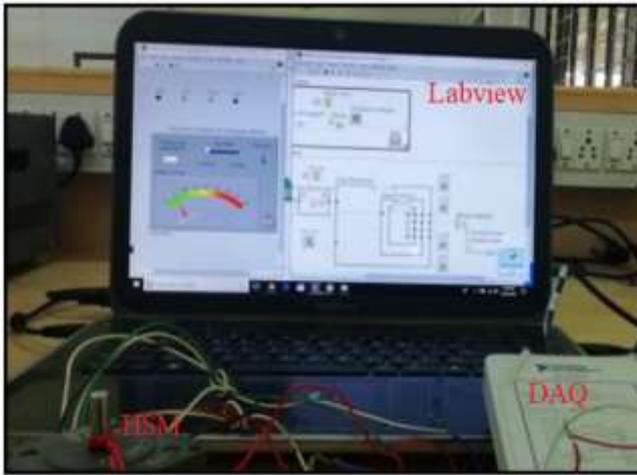


Figure 3. Physical Setup

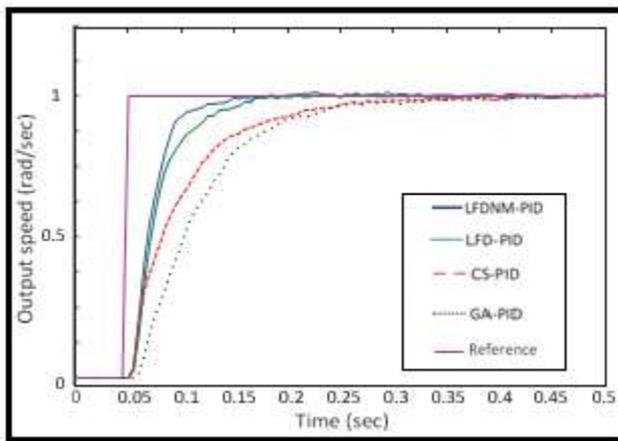


Figure 4. Experimental Performance Analysis

Table 6. Performance Parameters – Experimental Analysis

Time Domain Parameters	LFD-NM	LFD	CS	GA
M_p (%)	0.82	1.72	1.44	1.15
T_R (sec)	0.741	1.184	2.259	2.496
T_S (sec)	1.851	2.191	4.105	5.301
T_P (sec)	3.343	3.618	7.224	6.812

6. Conclusion

The benefits of the Levy flight distribution (LFD) and Nelder Mead (NM) algorithms are combined in this study to create a hybrid scheme. NM Simplex search method's enhanced localization capacity and LFD algorithm's broad search capability are combined in this hybrid approach. A hybrid stepper motor (HSM) speed regulator is constructed using an efficient proportional-integral-derivative (PID) controller utilising the suggested LFD-NM algorithm. Several comparison evaluations were carried out in order to assess the performance of the proposed LFD-NM-based PID controller. These comprised statistical tests, investigations of time domain analysis response & frequency domain

analysis response, robustness evaluations and load disturbance evaluations, and evaluation related to energy control signal. In comparison to PID controllers based on the LFD, CS, and GA, the results of these evaluations showed the LFD-NM algorithm-based PID controller to perform better. Conclusively, the research indicates that the LFD-NM algorithm provides a proficient method for developing a PID controller intended for integration into a hybrid stepper motor speed control system. The algorithm performs better than existing PID controllers tuning approaches in terms of rigidity, reliability, and performance features, suggesting potential applications in motor control systems.

Author Statements:

- **Ethical approval:** The conducted research is not related to either human or animal use.
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- **Data availability statement:** The data that support the findings of this study are available on request from the corresponding author. The data are not publicly available due to privacy or ethical restrictions.

References

- [1] Boys, Dunlop (1979). Economical stepper motors for speed-control applications. *IEEE Journal on Electric Power Applications*, 2(1), pp. 27-28. DOI: <https://doi.org/10.1049/ij-epa.1979.0004>
- [2] Hasanien (2011). FPGA implementation of adaptive ANN controller for speed regulation of permanent magnet stepper motor drives. *Energy Conversion and Management*, 52(2), pp. 1252-1257. DOI: <https://doi.org/10.1016/j.enconman.2010.09.021>
- [3] Butcher, Masi, Olivieri (2012). An extended hybrid stepper motor electrical model for sensorless drives. *2012 IEEE International on Instrumentation and Measurement Technology Conference (I2MTC)*, pp. 781-786. DOI: <https://doi.org/10.1109/I2MTC.2012.6229555>
- [4] Melkote, Khorrami (1997). A unified approach to adaptive nonlinear control of stepper motors. *Proceedings of the 36th IEEE Conference on*

- Decision and Control*, 3, pp. 2495-2500. DOI: <https://doi.org/10.1109/CDC.1997.657531>
- [5] Condit, Jones (2004). Stepping motors fundamentals. Ed: *Microchip Application Note: AN907*.
- [6] Bendjedia, Ait-Amirat, Walther, Berthon (2007). Sensorless control of hybrid stepper motor. *2007 European Conference on Power Electronics and Applications*, pp. 1-10. DOI: <https://doi.org/10.1109/EPE.2007.4417444>
- [7] Ellis (1971). Analysis and control of the permanent magnet stepper motor. *Radio and Electronic Engineer*, 41, pp. 302-308. DOI: <https://doi.org/10.1049/ree.1971.0091>
- [8] Tsui, Cheung, Yuen (2009). Novel Modeling and Damping Technique for Hybrid Stepper Motor. *IEEE Transactions on Industrial Electronics*, 56(1), pp. 202-211. DOI: <https://doi.org/10.1109/TIE.2008.2008791>
- [9] Tzung-Cheng, Yung-Chun (2008). High performance algorithm realization on FPGA for stepper motor controller. *2008 SICE Annual Conference*, pp. 1390-1395. DOI: <https://doi.org/10.1109/SICE.2008.4654875>
- [10] Hekimoglu (2019). Optimal tuning of fractional order PID controller for DC motor speed control via chaotic atom search optimization algorithm. *IEEE Access*, 7, pp. 38100-38114. DOI: <https://doi.org/10.1109/ACCESS.2019.2905961>
- [11] Rodriguez-Molina, Villarreal-Cervantes, Aldape-Perez (2019). An adaptive control study for the DC motor using meta-heuristic algorithms. *IFAC-PapersOnLine*, 23(3), pp. 889-906. DOI: <https://doi.org/10.1016/j.ifacol.2017.08.2164>
- [12] Pal, Mukherjee, Bhakta (2020). Design of an intelligent heuristic algorithm-based optimised fuzzy controller for speed control of a separately excited DC motor. *Australian Journal of Electrical and Electronics Engineering*, 17(3), pp. 173-182. DOI: <https://doi.org/10.1080/1448837X.2020.1804678>
- [13] Lotfy, Kaveh, Mosavi, Rahmati (2020). An enhanced fuzzy controller based on improved genetic algorithm for speed control of DC motors. *Analog Integrated Circuits and Signal Processing*, 105, pp. 141-155. DOI: <https://doi.org/10.1007/s10470-020-01599-9>
- [14] Premkumar, Manikandan (2015). Speed control of brush-less DC motor using bat algorithm optimized adaptive neuro-fuzzy inference system. *Applied Soft Computing Journal*, 32, pp. 403-419. DOI: <https://doi.org/10.1016/j.asoc.2015.04.014>
- [15] Ahmed, Rajoriya (2017). A hybrid of sliding mode control and fuzzy logic control using a fuzzy supervisory switched system for DC motor speed control. *Turkish Journal of Electrical Engineering & Computer Sciences*, 25(3), p. 30. DOI: <https://doi.org/10.3906/elk-1511-213>
- [16] Bhatt, Parmar, Gupta, Sikander (2019). Application of stochastic fractal search in approximation and control of LTI systems. *Microsystem Technologies*, 25(1), pp. 105-114. DOI: <https://doi.org/10.1007/s00542-018-3939-6>
- [17] Puangdownreong, Nawikavatan, Thammarat (2016). Optimal design of I-PD controller for DC motor speed control system by cuckoo search. *Procedia Computer Science*, 86, pp. 83-86. DOI: <https://doi.org/10.1016/j.procs.2016.05.021>
- [18] Akbari-Hasanjani, Javadi, Sabbaghi-Nadooshan (2015). DC motor speed control by self-tuning fuzzy PID algorithm. *Transactions of the Institute of Measurement and Control*, 37(2), pp. 164-176. DOI: <https://doi.org/10.1177/0142331214535619>
- [19] Kalpana K, Paulchamy B, Stephen Jeswinde Nuagah, Piyush Kumar Shukla., (2023), Design of a high-performance advanced phase locked loop with high stability external loop filter, *IET Circuits Devices Systems*, 17(1);1-12.
- [20] Kumar, Chatterjee Shantanu Shah, Saha, Saibal Chatterjee (2017). On comparison of tuning method of FOPID controller for controlling field controlled DC servo motor. *Cogent Engineering*, 4(1). DOI: <https://doi.org/10.1080/23311916.2017.1357875>
- [21] Mishra, Singh, Yadav (2020). Design of optimal PID controller for varied system using teaching-learning-based optimization. *Advances in Computing and Intelligent Systems*, Springer, pp. 153-163. DOI: https://doi.org/10.1007/978-981-15-0222-4_13
- [22] Pongfai, Su, Zhang, Assawinchaichote (2020). A novel optimal PID controller autotuning design based on the SLP algorithm. *Expert Systems*, 37(2). DOI: <https://doi.org/10.1111/exsy.12489>
- [23] Hekimoglu (2019). Speed control of DC motor using PID controller tuned via kidney-inspired algorithm. *BEU Journal of Science*, 8(2), pp. 652-663. DOI: <https://doi.org/10.17798/bitlisfen.496782>
- [24] Mohamed, Abubakr, Alamin, Hassan (2020). Modified WCA-based adaptive control approach using balloon effect: Electrical systems applications. *IEEE Access*, 8, pp. 60877-60889. DOI: <https://doi.org/10.1109/ACCESS.2020.2982510>
- [25] Sabir, Khan (2014). Optimal design of PID controller for the speed control of DC motor by using metaheuristic techniques. *Gastaldo P (ed) Advances in Artificial Neural Systems*, Hindawi Publishing Corporation, pp. 1-8. DOI: <https://doi.org/10.1155/2014/126317>
- [26] Ekinci, Izci, Hekimoglu (2020). PID speed control of DC motor using Harris hawks optimization algorithm. *2020 IEEE International Conference on Electrical, Communication, and Computer Engineering (ICECCE)*, pp. 1-6. DOI: <https://doi.org/10.1109/ICECCE49384.2020.9179308>
- [27] Serradilla, Canas, Naranjo (2020). Optimization of the energy consumption of electric motors through metaheuristics and PID controllers. *Electronics*, 9(11), p. 1842. DOI: <https://doi.org/10.3390/electronics9111842>
- [28] Duman, Maden, Guvenxc (2011). Determination of the PID controller parameters for speed and position control of DC motor using gravitational search algorithm. *ELECO 2011 - 7th International Conference on Electrical and Electronics Engineering*, pp. I-225-I-229.

- [29] Potnuru, Alice Mary, Sai Babu (2019). Experimental implementation of flower pollination algorithm for speed controller of a BLDC motor. *Ain Shams Engineering Journal*, 10(2), pp. 287–295. DOI: <https://doi.org/10.1016/j.asej.2018.07.005>
- [30] Bhatnagar, Gupta (2018). Application of grey wolf optimization in optimal control of DC motor and robustness analysis. *Skit Research Journal*, 8(1), pp. 19–25. DOI: <https://doi.org/10.479004/IJSKIT.8.1.2018.19-25>
- [31] Khalilpour, Razmjoo, Moallem (2011). Optimal control of DC motor using invasive weed optimization (IWO) algorithm. *Majlesi Conference on Electrical Engineering*.
- [32] El-Deen, Hakim Mahmoud, El-Sawi (2015). Optimal PID tuning for DC motor speed controller based on genetic algorithm. *International Review of Automatic Control*, 8(1), pp. 80–85. DOI: <https://doi.org/10.15866/ireaco.v8i1.4839>
- [33] Khanam, Parmar (2017). Application of SFS algorithm in control of DC motor and comparative analysis. *2017 4th IEEE Uttar Pradesh Section International Conference on Electrical, Computer and Electronics, UPCON 2017*, pp. 256–261. DOI: <https://doi.org/10.1109/UPCON.2017.8251057>
- [34] Kouassi, Zhang, Mbyamm Kiki, Ouattara (2020). Speed control of brushless de motor using ant colony optimization. *IOP Conference Series: Earth and Environmental Science*, 431(1). DOI: <https://doi.org/10.1088/1755-1315/431/1/012022>
- [35] Agarwal, Parmar, Gupta (2018). Comparative analysis of PID controller for speed control of DC motor with intelligent optimization algorithms. *Proceedings - IEEE 2018 International Conference on Advances in Computing, Communication Control and Networking, ICACCCN 2018*, pp. 273–277. DOI: <https://doi.org/10.1109/ICACCCN.2018.8748475>
- [36] Ekinci, Hekimoglu, Demiroren, Eker (2019). Speed control of DC motor using improved sine cosine algorithm based PID controller. *2019 3rd International Symposium on Multidisciplinary Studies and Innovative Technologies (ISMSIT 2019)*, pp. 1–7. DOI: <https://doi.org/10.1109/ISMSIT.2019.8932907>
- [37] Izci, Ekinci (2021). Comparative performance analysis of slime mould algorithm for efficient design of proportional–integral– derivative controller. *Electrica*, 21(1), pp. 151–159. DOI: <https://doi.org/10.5152/electrica.2021.20077>
- [38] Eker, Kayri, Ekinci, Izci (2021). A new fusion of ASO with SA algorithm and its applications to MLP training and DC motor speed control. *Arabian Journal for Science and Engineering*, 46, pp. 3889–3911. DOI: <https://doi.org/10.1007/s13369-020-05228-5>
- [39] Wolpert, Macready (1997). No free lunch theorems for optimization. *IEEE Transactions on Evolutionary Computation*, 1(1), pp.67–82. DOI: <https://doi.org/10.1109/4235.585893>
- [40] Houssein, Saad, Hashim, Shaban, Hassaballah (2020). Levy flight distribution: A new metaheuristic algorithm for solving engineering optimization problems. *Engineering Applications of Artificial Intelligence*, 94, p. 103731. DOI: <https://doi.org/10.1016/j.engappai.2020.103731>
- [41] Nelder, Mead (1965). A simplex method for function minimization. *The Computer Journal*, 7(4), pp. 308–313. DOI: <https://doi.org/10.1093/COMJNL%2F7.4.308>
- [42] Izci, Ekinci, Orenc, et al. (2020). Improved artificial electric field algorithm using Nelder Mead simplex method for optimization problems. *2020 4th International Symposium on Multidisciplinary Studies and Innovative Technologies (ISMSIT)*, pp. 1–5. DOI: <https://doi.org/10.1109/ISMSIT50672.2020.9255255>
- [43] Lagarias, Reeds, Wright, Paul (1998). Convergence properties of the Nelder Mead simplex method in low dimensions. *SIAM Journal on Optimization*, 9(1). DOI: <https://doi.org/10.1137/S1052623496303470>
- [44] Xu, Wang, Liu (2018). Parameter estimation for chaotic systems via a hybrid flower pollination algorithm. *Neural Computing and Applications*, 30(8), pp. 2607–2623. DOI: <https://doi.org/10.1007/s00521-017-2890-2>
- [45] Xu, Wang (2017). Parameter estimation of photovoltaic modules using a hybrid flower pollination algorithm. *Energy Conversion and Management*, 144, pp. 53–68. DOI: <https://doi.org/10.1016/j.enconman.2017.04.042>
- [46] Xu, Wang, Wang (2019). Parameter estimation of proton exchange membrane fuel cells using eagle strategy based on JAYA algorithm and Nelder Mead simplex method. *Energy*, 173, pp. 457–467. DOI: <https://doi.org/10.1016/j.energy.2019.02.106>
- [47] Fakhouri, Hudaib, Sleit (2020). Hybrid particle swarm optimization with sine cosine algorithm and Nelder–Mead simplex for solving engineering design problems. *Arabian Journal for Science and Engineering*, 45(4), pp. 3091–3109. DOI: <https://doi.org/10.1007/s13369-019-04285-9>
- [48] Yildiz (2019). A novel hybrid whale–Nelder–Mead algorithm for optimization of design and manufacturing problems. *The International Journal of Advanced Manufacturing Technology*, 105(12), pp. 5091–5104. DOI: <https://doi.org/10.1007/s00170-019-04532-1>
- [49] Blondin, Sanchis, Sicard, Herrero (2018). New optimal controller tuning method for an AVR system using a simplified ant colony optimization with a new constrained Nelder–Mead algorithm. *Applied Soft Computing*, 62, pp. 216–229. DOI: <https://doi.org/10.1016/j.asoc.2017.10.007>
- [50] Chen, Yu (2020). A hybrid ant lion optimizer with improved Nelder–Mead algorithm for structural damage detection by improving weighted trace lasso regularization. *Advances in Structural Engineering*, 23(3). DOI: <https://doi.org/10.1177/1369433219872434>
- [51] Rizk-Allah, Hassanien (2020). A hybrid Harris hawks- Nelder Mead optimization for practical nonlinear ordinary differential equations.

- Evolutionary Intelligence*, 15, pp. 141–165. DOI: <https://doi.org/10.1007/s12065-020-00497-3>
- [52] Singh, Elaziz, Xiong (2018). Modified spider monkey optimization based on Nelder–Mead method for global optimization. *Expert Systems with Applications*, 110, pp. 264–289. DOI: <https://doi.org/10.1016/j.eswa.2018.05.040>
- [53] Xu, Yan (2019). Hybrid Nelder–Mead algorithm and dragon- fly algorithm for function optimization and the training of a multilayer perceptron. *Arabian Journal for Science and Engineering*, 44(4), pp. 3473–3487. DOI: <https://doi.org/10.1007/s13369-018-3536-0>
- [54] Yıldız , Betül Sultan Yıldız , Sadiq Sait , Sujin Bureerat, Nantiwat Pholdee (2019). A new hybrid Harris hawks-Nelder Mead optimization algorithm for solving design and manufacturing problems. *Materials Testing*, 61(8), pp. 735–743. DOI: <https://doi.org/10.3139/120.111378>
- [55] Zhang, Heidari, Wang, Zhang, Chen, Chengye (2020). Orthogonal Nelder Mead moth flame method for parameters identification of photovoltaic modules. *Energy Conversion and Management*, 211, p. 112764. DOI: <https://doi.org/10.1016/j.enconman.2020.112764>
- [56] Gaing (2004). A particle swarm optimization approach for optimum design of PID controller in AVR system. *IEEE Transactions on Energy Conversion*, 19(2), pp. 384–391. DOI: <https://doi.org/10.1109/TEC.2003.821821>
- [57] Ogata (2010). *Modern Control Engineering. 5th Ed. New Jersey: Prentice-Hall.*
- [58] Yang, Deb (2009). Cuckoo search via Levy flights. *NABIC 2009 - Proceedings 2009 World Congress on Nature and Biologically Inspired Computing*, pp. 210–214. DOI: <https://doi.org/10.1109/NABIC.2009.5393690>
- [59] Holland (1992). Genetic algorithms. *Scientific American*, 267(1), pp. 66-73.